Final Exam Information

- Exam time is 5:30pm on Wednesday, December 10th
- The final exam is cumulative: define p-value, three short questions over material from exam 1, one long question like long questions on exam 2 or first long question on exam 3, one long question combining the material from the second and third long question on exam 3, and one long question like the one below.

New Material from Chapter 13 - Contingency Tables

Goodness of fit test
Test for Independence
Test for Homogeneity

How big does the sample size need to be for the $\chi^2$ test to work?
(at least 80% of expected values 5, none less than 1)
\[\text{df} = \# \text{ cells} - \# \text{ fixed cells} - \# \text{ estimated parameters}\]

You will get copies of the formula sheets from the first three exams, as well as $\sum \frac{(\text{Obs} - \text{Exp})^2}{\text{Exp}}$

Sample Exam Questions over This Material

1) It is desired to test that a die is fair. (So each of the six sides has the same chance of coming up). What is the minimum number of times we could roll the die to test it and still have the assumptions of the Chi-squared goodness of fit test met?

2) A survey is conducted to determine which type of media various age groups think are most credible.

<table>
<thead>
<tr>
<th></th>
<th>Newspaper</th>
<th>Television</th>
<th>Radio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Under 35</td>
<td>30</td>
<td>68</td>
<td>10</td>
</tr>
<tr>
<td>35-54</td>
<td>61</td>
<td>79</td>
<td>20</td>
</tr>
<tr>
<td>Over 54</td>
<td>98</td>
<td>43</td>
<td>21</td>
</tr>
</tbody>
</table>

a) What would the degrees of freedom be for testing the null hypothesis that age is independent of most trusted news medium?

b) For testing the null hypothesis that age is independent of most trusted news medium, what is the expected number of people between ages 35 and 54 who find television most credible?

c) A previous study found for people under age 35 that 20% considered Newspapers most credible, 75% considered Television most credible, and 5% considered Radio most credible. Test the hypothesis that the findings of the survey above agree with these percentages for people under age 35. (Use $\alpha=0.05$)

Answers:

1) 6x5=30 would give an expected value of 5 for each side.
2a) df=(#row-1)(#col-1)=(3-1)(3-1)=2x2=4
2b) $\text{rc/n} = (61+79+20)(68+79+43)/(30+68+10+61+79+20+98+43+21)=70.698$
2c) This is a goodness of fit test.
   \[\text{Obs}=[30 \ 68 \ 10] \quad \text{Exp}=[0.20x108 \ 0.75x108 \ 0.05x108] = [21.6 \ 81 \ 5.4]\]
   \[\chi^2=(30-21.6)^2/21.6 + (68-81)^2/81 + (10-5.4)^2/5.4 = 9.27 \ \text{compare to 5.99 (df=2) and reject H}_0.\]