

STAT 703/J703
January 16th, 2007

Instructor: Brian Habing
Department of Statistics
LeConte 203
Telephone: 803-777-3578
E-mail: habing@stat.sc.edu



Today

- Syllabus
- Solutions to the 702 Final



1) Assume SAT verbal scores have mean 505 and standard deviation 111, and SAT math scores have mean 511 and standard deviation 114, and the correlation between the scores is 0.479. Find the mean and standard deviation of the total scores (verbal + math).



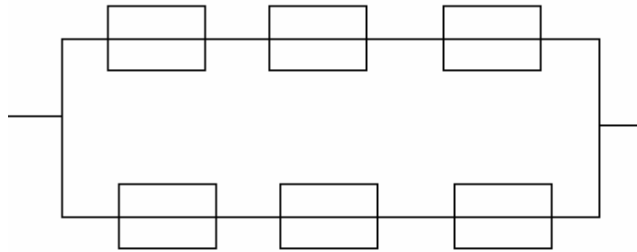
2) Find the third and fourth moments for a standard normal random variable (you may use the formulas for the m.g.f. or p.d.f. of a normal, but must show all other work).



3) Use moment generating functions to show that the sum of M (an integer greater than one) independent geometric random variables with parameter p are distributed as a negative binomial. Be sure to specify the parameters of the negative binomial.



4) Each component in the system shown below has probability p of failing. Find the probability that the system fails.



5) A system has 8 components whose failure time follow an exponential distribution with $\lambda=1$. The system is designed so that it will still function when one of the components fail. That is, it fails when at least 2 of the components fail. Show that the pdf of the time until the system fails is $f(t)=56[\exp(-7t)-\exp(-8t)]$



6) Consider sampling from a population of size 10,000 that could be broken into strata of sizes 5000, 3000, 1000, and 1000 respectively. Assume 10% of the population has the socio-economic trait we are interested in (the percentages in the sub-strata are 1%, 5%, 10%, and 70%)...



A sample of size 400 is to be taken by one of three sampling schemes: a simple random sample, a stratified random sample with 100 being sampled from each strata, and a stratified random sample with sizes 200, 120, 40, and 40 respectively. Find the variance of the estimated percentage for each of these sampling schemes.



7) Say we want to make a simple model for the total number of yards St. Louis Rams wide receiver Torrey Holt will gain in a game. Assume the number of receptions follows a Poisson distribution with $\lambda=5$, and the number of yards on each reception follows a gamma distribution with $\alpha=1.2$ and $\lambda=0.08$. Find the mean and variance for the total yards per game.



8) If X_n is a sequence of χ^2 random variables each with n degrees of freedom, briefly explain what happens to X_n/n as $n \rightarrow \infty$.



9) Assume that a standardized test has a mean score of 511 and the standard deviation is 114, but nothing else is reported about the distribution. What is the largest percentage of students who could have scored 800 (or higher)?



10) Assume that a standardized test has a mean score of 511 and a standard deviation of 114. A random sample of 500 examinees is taken. Estimate the probability that the average test score of these 500 students will be greater than 525.



11) Assume X_1, \dots, X_n are an i.i.d. sample from a normal population with mean μ and variance σ^2 . What is the probability that you would observe a sample variance of 6.4 or larger if the true population variance was only 5.8. (Hint: `pnorm`, `pchisq`, and `pf` can be used to get the cumulative distribution functions for the normal, chi-square, and F distributions respectively. Use `help(pnorm)`, for example, for more information.) .



Next?

Chapter 8: Estimating Parameters

