## Assessment of DPOAE Test-Retest Difference Curves via Hierarchical Gaussian Processes

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Cisplatin

DPOAE Data Gaussian processes

#### • Cisplatin: chemotherapeudic agent, treats many cancers.

- Can cause ototoxicity: inner ear poisoning & hearing loss.
- Cisplatin chemotherapy causes permanent hearing loss in approximately 70% of children and adolescents.
- Serial monitoring via hearing tests used to assess severe ototoxicity.
- Hearing tests difficult or impossible for very young or very ill cancer patients.

DPOAE

DPOAE Data Gaussian processes

# Distortion production otoacoustic emissions (DPOAE)

- testing is a promising, non-invasive alternative to behavioral hearing tests.
- OAE elicited by sealing a small speaker & microphone in ear canal and playing tone through speaker.
- Pairs of tones (primary frequency 'f2' & secondary) frequency) generate 'distortion product' OAE, or DPOAE, measured by microphone.
- Most common clinical protocol: play tones at successively increasing f2 and measure DPOAE.
- Generates 'DP-gram' that an audiologist can use to evaluate the health of the cochlea

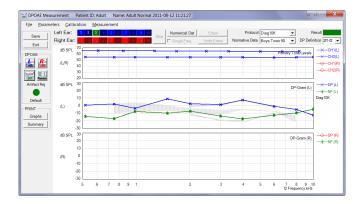
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## DPOAE testing on infant



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## DPOAE test result on healthy adult



From Mimosa Acoustics webpage.

 Background
 DPOAE

 Hierarchical mixed model
 Data

 Generalizations and simplifications
 Gaussia

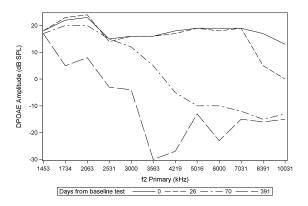
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## **DP-grams**

- DP-grams measured every 3, 4, or 6 weeks show how the cochlea is changing; if significant change observed, course of chemotherapty can be altered.
- Theoretically, each human has smooth DP-gram as a function of f2 at any given time and for a given ear.
- DP-grams change over time and from left to right ear.
- Currently six DPOAE systems in widespread use; typical f2's are 1, 2, 3, 4, 6, and 8 kHz, but others are used depending on system and user.
- Statistical problem: provide normal ranges for test-retest differences, i.e. difference in DP-grams from baseline to followup for normal healthy children.
- Challenge: DP-grams correlated across f2, time, and ear.

## DP-grams: 1.5 year old treated with cisplatin

DP-grams for 18 month-old male cancer patient at baseline & about 4, 10, and 56 weeks later.



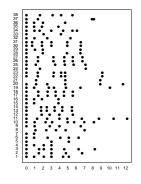
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## Data collected

- n = 38 healthy children aged 10 years or younger recruited from Oregon Health and Science University Doernbecher Children's Hospital between February 2006 and July 2009
- Subjects have normal hearing sensitivity; measurable DPOAEs; no history of ototoxic treatment, ear pathology, ear surgery, or tympanostomy tubes.
- Test sessions excluded for conductive hearing loss, abnormal tympanometry, or excessive subject noise or non-cooperation.
- DPOAES measured twelve f2 primaries from 1453 to 10031 Hz in half octave steps and using L2/L1 = 65/55 dB SPL and f2/f1 ratio of 1.22.
- Children retested at different times, at different frequencies, and possibly either one or both ears; high degree of unbalance.

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## When followup DPOAE were collected



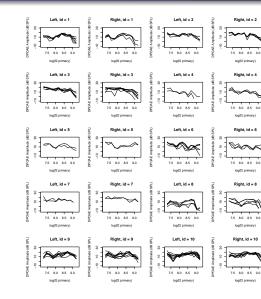
Months from baseline

#### Features of the dataset

- Two subjects provided no valid baseline data.
- There is quite a bit of variation in the number of followups and the followup intervals.
- Most data only cover up to about 7 months of followup.

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## DP-grams for 10 subjects



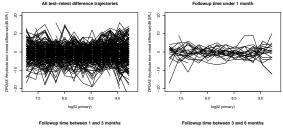
#### Features of the DP grams

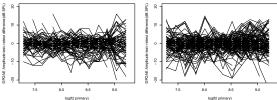
- 'Intercept' & 'slope' quite different.
- Overall common shape: decreasing-increasingdecreasing.
- Strong correlation within subject over time & ear.
- Variability remarkably constant within subject.

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DPOAE Data Gaussian processes

## Test-retest differences by followup time





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## Data & notation

- Data collected over differing frequencies, at different followup times, and for one or both ears; indexing is a nightmare.
- Had to consider different indexing for different models. Hardest part: data manipulation & bookkeeping.
- *i* = 1, ..., 38 subjects.
- Subject *i* seen at *potentially j* = 1,..., 12 different log-f2
   **f** = (f<sub>1</sub>,..., f<sub>12</sub>)' over *all* followup times.
- Subject *i* observed at *T<sub>i</sub>* times including baseline:
   t<sub>i</sub> = t<sub>i1</sub>,..., t<sub>iT<sub>i</sub></sub>.

DPOAE Data Gaussian processes

## Gaussian processes

- Gaussian processes becoming very popular for modeling functions nonparametrically. Small number of parameters control smoothness properties.
- Nice video tutorial at

http://videolectures.net/gpip06\_mackay\_gpb/

- Competitor to splines, neural networks, harmonic expansions; includes many approaches as special case.
- Main problem: computation O(s<sup>3</sup>). For us s ≤ 200; usually much smaller.

## Gaussian process in one dimension

Stochastic process e(t) s.t. the function e(t) observed at (t<sub>1</sub>,..., t<sub>s</sub>)' is multivariate normal, e.g.

$$(\boldsymbol{e}(t_1),\ldots,\boldsymbol{e}(t_s))'\sim N_{\mathcal{S}}\{\boldsymbol{0},\boldsymbol{\Sigma}(t_1,\ldots,t_s)\}.$$

- Only need covariance function  $\sigma(s, t) = \text{cov}(e(s), e(t))$ .
- Used here: squared exponential  $\sigma(s, t) = \sigma^2 \exp(-\theta |s t|^2)$ . Smoothness parameter  $\theta$  subject-specific later on.
- Generalizes to frequency & ear too: *e*(*t*, *f*, *l*). Two surfaces in ℝ<sup>2</sup> for each subject, one for each ear.
- Since only a finite number of responses *can ever* be recorded, likelihood is product of multivariate normal kernels; easy to work with.

Hierarchical Gaussian process regression model

Consider mixed model

$$y_{ijkl} = \mu(f_j) + b_{i0} + b_{i1}f_j + e_{ijkl},$$

where

- $i = 1, \ldots, 38$  indexes subject.
- $j = 1, \ldots, 12$  indexes frequency level.
- $k = 1, ..., T_i$  indexes the visit time for subject *i*.
- I = 1, 2; I = 1 is left ear & I = 2 right.
- Overall pop'n curvy  $\mu(f)$  plus subject specific line  $b_{i0} + b_{i1}f$ .
- *e<sub>ijkl</sub>* is Gaussian process over f2, time, and ear for *i* observed at finite number of points.
- $E(b_{i0}) = \beta_0$ ,  $E(b_{i1}) = \beta_1$  and  $E(e_{ijkl}) = 0$ .

## Population mean $\mu(f)$ is penalized B-spline

Easy to work with in mixed model context!

$$u(f) = \sum_{s=1}^{S} \gamma_s \phi_s(f).$$

- Knots equispaced over range of log f2 primary levels in the data and S = 20 basis functions used.
- Since  $\mu(f)$  includes constant or linear functions as special case, mean  $\beta_0 + \beta_1 f + \mu(f)$  overspecified unless constraints introduced. Set two of the B-spline coefficients to zero,  $\gamma_1 = \gamma_S = 0$  (Gray, 1992).

## Population mean $\mu(f)$ is penalized B-spline

The B-spline parameters are  $\gamma = (\gamma_2, \dots, \gamma_{S-1})'$ , given a 2nd-order random-walk prior

$$p(oldsymbol{\gamma}) \propto \lambda^{rac{S-2}{2}} \exp\{-0.5\lambda \| oldsymbol{D} oldsymbol{\gamma} \|^2\},$$

where **D** is a  $(S-4) \times (S-2)$  penalty matrix. Following Lang and Brezger (2004), the penalty parameter  $\lambda$  follows

$$\lambda \sim \Gamma(\alpha_1, \alpha_2),$$

with  $\alpha_1 = 1$  and  $\alpha_2 = 0.005$  or 0.0005.

Hierarchical Gaussian process Reference charts & contour probabilities

## Building a linear model

#### Let

$$\begin{aligned} \mathbf{X}_{ijk} &= \mathbf{1}_{L_{ijk}} \otimes (\phi_2(f_j), \dots, \phi_{S-1}(f_j)) \\ \mathbf{X}_{ij} &= [\mathbf{X}'_{ij1} \cdots \mathbf{X}'_{ijT_i}]' \\ \mathbf{Z}_{ijk} &= \mathbf{1}_{L_{ijk}} \otimes (1, f_j) \\ \mathbf{Z}_{ij} &= [\mathbf{Z}'_{ij1} \cdots \mathbf{Z}'_{ijT_i}]' \end{aligned}$$

Each child's vector of responses at frequency level  $f_j$  follows linear model

$$\mathbf{y}_{ij} = \mathbf{X}_{ij}\boldsymbol{\gamma} + \mathbf{Z}_{ij}\boldsymbol{b}_i + \boldsymbol{e}_{ij},$$

for i = 1, ..., 38 and j = 1, ..., 12. These vectors are of differing lengths!  $L_{ijk}$  is 0, 1, or 2; number of ears looked at for subject *i* at frequency *j* & time  $t_{ik}$ .

## Child-specific deviation from the population trend

- Each child's ear-specific response surface y<sub>il</sub>(t, f) deviates from the population mean β<sub>0</sub> + β<sub>1</sub>f + μ(f) by a smooth mean-zero surface in time and frequency (b<sub>i0</sub> - β<sub>0</sub>) + (b<sub>i1</sub> - β<sub>1</sub>)f + e<sub>il</sub>(t).
- Define *e*<sub>ij</sub> = (*e*'<sub>ij1</sub>,..., *e*'<sub>ijTi</sub>)' for child *i* at f2 level *j*. The Gaussian process model assumes

$$oldsymbol{e}_{ij} \stackrel{\textit{ind.}}{\sim} N_{n_{ij}}(oldsymbol{0}, oldsymbol{\Sigma}_{ij}),$$

where  $\Sigma_{ij}$  is the covariance matrix of  $\boldsymbol{e}_{ij}$  with separable covariance structure

$$\operatorname{cov}(e_{ijkl}, e_{ijk'l'}) = \sigma_i^2 \exp\{-\theta_{ti}|t_{ijk} - t_{ijk'}|^2 - \theta_{ei}|l-l'|^2\}.$$

 If both ears are measured at the same time points at each f2 frequency level, subject-specific covariance is

$$oldsymbol{e}_{ij} \sim oldsymbol{N}_{n_{ij}}(oldsymbol{0}, \sigma_i^2 oldsymbol{\Sigma}_{ti} \otimes oldsymbol{\Sigma}_{ei}).$$

Subject-specific smoothness parameters and lines

- For each subject *i*, let  $\mathbf{r}_i = (\mathbf{b}'_i, \mathbf{v}'_i)'$  where  $\mathbf{b}_i = (b_{i0}, b_{i1})'$  and  $\mathbf{v}_i = (\log(\sigma_i^2), \log(\theta_{i1}), \log(\theta_{ei}))'$ .
- Based on preliminary non-hierarchical individual fits in SAS' proc mixed, multivariate normality is reasonable for r<sub>i</sub>:

$$\mathbf{r}_{1},\ldots,\mathbf{r}_{n}\mid\boldsymbol{\mu}_{r},\boldsymbol{\Sigma}_{r}\overset{iid}{\sim}\mathcal{N}_{5}(\boldsymbol{\mu}_{r},\boldsymbol{\Sigma}_{r}), \tag{1}$$

where

$$\mu_r = \left[ \begin{array}{c} \beta \\ \tau \end{array} \right], \ \Sigma_r = \left[ \begin{array}{c} \Sigma_b & \Sigma_{bv} \\ \Sigma'_{bv} & \Sigma_v \end{array} \right]$$

Population parameters have prior

$$\mu_r \sim N_5(\textbf{\textit{m}}_0, \textbf{\textit{M}}_0), \ \Sigma_r^{-1} \sim {\sf Wish}_5(\textbf{\textit{Q}}, q).$$

Hierarchical Gaussian process Reference charts & contour probabilities

## Hierarchical linear mixed model

$$\mathbf{y}_{ij} | \mathbf{b}_i, \mathbf{v}_i, \mathbf{\gamma} \sim N_{n_{ij}} (\mathbf{X}_{ij} \mathbf{\gamma} + \mathbf{Z}_{ij} \mathbf{b}_i, \mathbf{\Sigma}_{ij} (\mathbf{v}_i)),$$

$$(\mathbf{b}_i, \mathbf{v}_i) | \boldsymbol{\mu}_r, \boldsymbol{\Sigma}_r \sim N_5(\boldsymbol{\mu}_r, \boldsymbol{\Sigma}_r).$$

Priors placed on  $\mu_r$ ,  $\Sigma_r$ ,  $\gamma | \lambda$ , and  $\lambda$ .

Hierarchical Gaussian process Reference charts & contour probabilities

## Markov chain Monte Carlo

- Blocks of parameters have conjugate closed-form updates, other blocks updated via adaptive Metropolis-Hastings (Haario, Saksman, and Tamminen, 2001 & 2005). Details in paper.
- Fully 20,000 MCMC iterates were generated with the last 10,000 iterations used for posterior inference. Code written in FORTRAN 90 using IMSL library.
- During the last 10,000 iterations, a child's DP-gram was predicted from the *population*, consisting of responses corresponding to 31 log(f2 primary) levels.
- Based on these samples, both the pointwise and simultaneous 95% credible bands were generated for DP-grams of a randomly selected healthy child.

## One observation time, volume tube method

Let

y\* = (y<sub>1</sub>\*,..., y<sub>F\*</sub>\*)' be a vector of correlated responses from a random child drawn from the population at any time across the *F*\* frequencies f\* = (f<sub>1</sub>\*,..., f<sub>F\*</sub>\*)', for either ear

• 
$$\mathbf{Z}_{j}^{*} = (1, f_{j}^{*})$$
 and  $\mathbf{Z}^{*} = [\mathbf{Z}_{1}^{*'} \cdots \mathbf{Z}_{F^{*}}^{*'}]'$ 

• 
$$\mathbf{r}^* = (b_0^*, b_1^*, \log(\sigma^{2*}), \log(\theta_t^*), \log(\theta_e^*))'$$

• 
$$\Sigma^* = \sigma^{2*} I_{F^*}$$

Hierarchical model  $\Rightarrow$  random child's response sampled given  $(\mu_r, \Sigma_r, \gamma)$  by first sampling the subject-specific variables

$$\boldsymbol{r}^* \mid \boldsymbol{\mu}_r, \boldsymbol{\Sigma}_r \sim N_5(\boldsymbol{\mu}_r, \boldsymbol{\Sigma}_r),$$

followed by sampling the DP-gram

$$oldsymbol{y}^* \mid oldsymbol{r}^*, oldsymbol{\gamma} \sim oldsymbol{\mathcal{N}}_{F^*}(oldsymbol{X}^*oldsymbol{\gamma} + oldsymbol{Z}^*oldsymbol{b}^*, \Sigma^*).$$

One observation time, volume tube method

• Due to linearity, the mean of any y\* is simply

$$oldsymbol{\mu}^* = oldsymbol{\mathsf{X}}^*ar{\gamma} + oldsymbol{\mathsf{Z}}^*ar{oldsymbol{eta}}$$

 At each f2 frequency level, the usual equal-tailed pointwise (1 – α)100% credible interval is formed yielding upper and lower pointwise interval endpoints u<sub>1</sub>,..., u<sub>F\*</sub>, l<sub>1</sub>,..., l<sub>F\*</sub>, which are well-approximated by

$$u_j = y_j^{* \lceil (1 - \alpha/2)M \rceil}$$
 and  $l_j = y_j^{* \lceil (\alpha/2)M \rceil}$ 

• Each pointwise interval  $(I_j, u_j)$  is adjusted by increasing c > 1 to

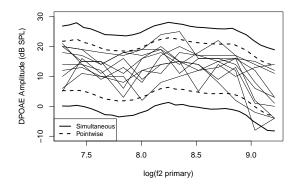
$$(\mu_j^* - c(\mu_j^* - l_j), \mu_j^* + c(u_j - \mu_j^*))$$

until exactly  $(1 - \alpha)100\%$  of the  $\mathbf{y}^{*1}, \ldots, \mathbf{y}^{*M}$  lie between the two adjusted bands.

Hierarchical Gaussian process Reference charts & contour probabilities

## One observation only

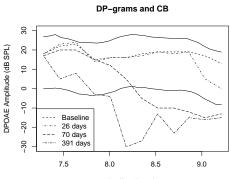
95% credible bands (both pointwise and simultaneous) & 10 sample DP-grams from data:



Hierarchical Gaussian process Reference charts & contour probabilities

## One observation only

#### Actual cancer patient:



log(f2 primary)

## Reference chart for DP-gram test-retest difference

- A 95% reference interval corresponds to the range of DPOAE level shifts that a clinician can reasonably expect to see in a healthy population.
- Let y<sub>1</sub><sup>\*</sup> = (y<sub>11</sub><sup>\*</sup>,..., y<sub>1F<sup>\*</sup></sub>)' and y<sub>2</sub><sup>\*</sup> = (y<sub>21</sub><sup>\*</sup>,..., y<sub>2F<sup>\*</sup></sub>)' be sets of emissions recorded on the same frequencies at times t<sub>1</sub> and t<sub>2</sub>, often baseline and then some months later.
- The difference at each frequency is given by the  $F^* \times 1$  vector  $\Delta = \begin{bmatrix} I & -I \end{bmatrix} (\mathbf{y}_1^{*'}, \mathbf{y}_2^{*'})'$ . A short calculation reveals that

$$\mathbf{\Delta} \sim \textit{N}_{\textit{F}^{*}}\left(\mathbf{0}, 2(1 - \exp\{- heta_{t}^{*}|t_{1} - t_{2}|^{2}\})\mathbf{\Sigma}^{*}
ight)$$

Hierarchical Gaussian process Reference charts & contour probabilities

## Posterior contour probabilities

- The simultaneous credible band provides a very quick check that a child's response is normal. However, it may miss DP-grams that are unusual in ways different than very high or low responses.
- Also useful to detecting abnormal test-retest differences.
- A contour probability measures how rare or unusual an observation is in a manner similar to a p-value.
- For continuous y ~ p(·), the contour probability for seeing an observation more unusual than y₀ is

 $P\{p(\mathbf{y}) < p(\mathbf{y}_0)\}$ 

## Posterior contour probabilities (continued)

• For one set of measurements contour probability for y<sub>0</sub> is

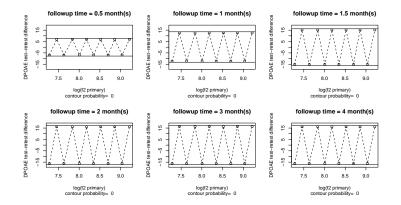
$$P\{p(\mathbf{y}^*) < p(\mathbf{y}_0)\} = \frac{1}{M} \sum_{m=1}^M P\{\chi_{F^*}^2 > (\mathbf{y}_0 - \mathbf{X}^* \boldsymbol{\gamma}^m - \mathbf{Z}^* \boldsymbol{b}^{*m})' [\boldsymbol{\Sigma}^{*m}]^{-1} (\mathbf{y}_0 - \mathbf{X}^* \boldsymbol{\gamma}^m - \mathbf{Z}^* \boldsymbol{b}^{*m})\}.$$

• Contour probability for difference of two DP-grams taken at two different visits on the same ear, say  $\Delta_0$ , is

$$P\{p(\Delta^*) < p(\Delta_0)\} = \frac{1}{M} \sum_{m=1}^{M} P\{\chi_{F^*}^2 > \Delta_0' [2(1 - e^{-\theta_t^{*m} |t_2 - t_1|^2}) \Sigma^{*m}]^{-1} \Delta_0'\}$$

Hierarchical Gaussian process Reference charts & contour probabilities

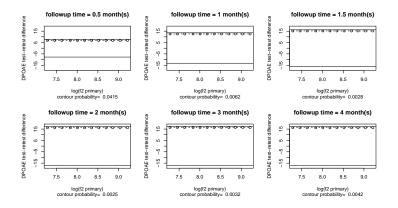
## Test-retest differences within band that are unusual



Differences that are too variable.

Hierarchical Gaussian process Reference charts & contour probabilities

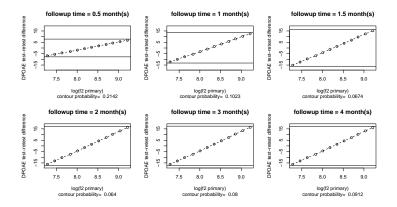
## Test-retest differences within band that are unusual



Vertical shift that falls within band.

Hierarchical Gaussian process Reference charts & contour probabilities

## Test-retest differences within band that are unusual



DP-grams that cross in the middle.

Hierarchical Gaussian process Reference charts & contour probabilities

## Bands & contour probabilities for some trajectories

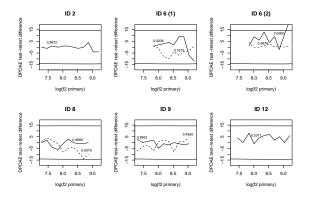
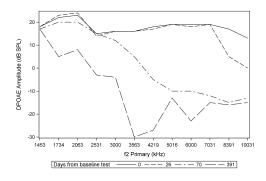


Figure: 10 sample DP-grams of test-retest differences of 5 children and 95% simultaneous credible band; followup time = 1 month.

## Data analysis: out-of-sample prediction for actual cancer patient

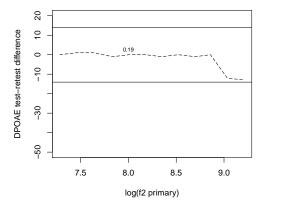
18 month-old male cancer patient's DP-grams from background; posterior mean contour probabilities at 26, 70, and 391 days after baseline are 0.19, 0.00, and 0.00 for the hierarchical model.



Hierarchical Gaussian process Reference charts & contour probabilities

## Test-retest difference

#### Actual cancer patient, first followup time.

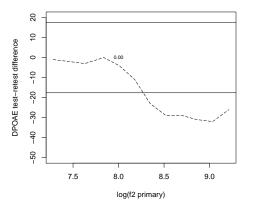


#### followup time = 26 days

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## Test-retest difference

#### Actual cancer patient, second followup time.

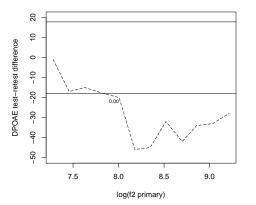


followup time = 70 days

Hierarchical Gaussian process Reference charts & contour probabilities

## **Test-retest difference**

#### Actual cancer patient, third followup time.



followup time = 391 days

Age-gender specific model Generalizations & simplications Conclusion

## Age-gender specific model

- There is a well-known physiological basis for an age effect on OAE amplitude: DPOAE amplitude decreases over the first few years of life as the ear canal gets larger and the nervous system matures.
- Since DPOAE levels naturally change with cochlear development, it is desirable to have age-appropriate DPOAE level shift standards as necessary.
- In general, we allow intercepts, slopes, and all three subject-specific variance components to change smoothly with age and gender, yeilding a Gaussian process structural equation model.

Age-gender specific model Generalizations & simplications Conclusion

Age-gender specific model (continued)

Let  $\boldsymbol{a}_i$  be a  $p \times 1$  vector of baseline covariates associated with child *i*; the hierarchical model becomes

$$\mathbf{r}_i \mid \boldsymbol{\mu}_r, \boldsymbol{\Sigma}_r \stackrel{ind}{\sim} N_5(\boldsymbol{\mu}_r \boldsymbol{a}_i, \boldsymbol{\Sigma}_r),$$

where

$$\mu_r = \left[ egin{array}{c} m{b}' \ m{ au}' \end{array} 
ight], \ m{\Sigma}_r = \left[ egin{array}{c} \Sigma_b & \Sigma_{bv} \ \Sigma_{bv}' & \Sigma_v \end{array} 
ight]$$

and

$$\mathbf{b}' = \begin{bmatrix} \beta_{11} & \cdots & \beta_{1p} \\ \beta_{21} & \cdots & \beta_{2p} \end{bmatrix} \text{ and } \mathbf{\tau}' = \begin{bmatrix} \tau_{11} & \cdots & \tau_{1p} \\ \tau_{21} & \cdots & \tau_{2p} \\ \tau_{31} & \cdots & \tau_{3p} \end{bmatrix}$$

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## Data analysis: age-gender-specific model

- The age-gender-specific model was also fit to the DPOAE data.
- By allowing subject-specific intercept-slope and Gaussian process variance components to be covariate-dependent, the structural equation model may have better predictive power than the hierarchical one, provided that baseline covariate information is available.
- However, in this data analysis, the log-pseudo marginal likelihood (LPML) of the age-gender-specific model is almost the same as that of the hierarchical model.

Age-gender specific model Generalizations & simplications Conclusion

## Data analysis: age-gender-specific model (continued)

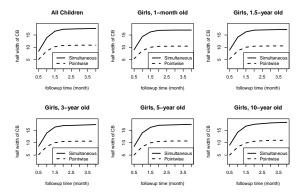


Figure: Half widths of credible bands of test-retest differences for all children and for girls.

Age-gender specific model Generalizations & simplications Conclusion

## Data analysis: age-gender-specific model (continued)

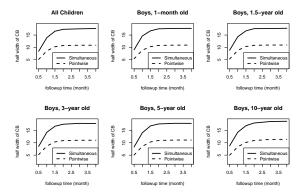


Figure: Half widths of credible bands of test-retest differences for all children and for boys.

## Data analysis: age-gender-specific model (continued)

- The previous two figures show that as followup time increases, the credible band tends to be wider.
  - The width of the credible band increases quickly as followup time goes from half a month to two months.
  - After two months, the curve is essentially static, i.e. temporal correlation dies down to almost zero.
- As the children get older, the credible band tends to be wider, reflecting more variability in DPOAE response.
- Boys have wider credible bands than girls at the same age with the same followup time.

Age-gender specific model Generalizations & simplications Conclusion

## Other models

In addition to the two models mentioned previously, we fit four more models:

- Hierarchical model with correlation among f2 frequency levels,
   i.e. subject-specific surfaces e<sub>il</sub>(f, t).
- Age-gender-specific model with correlation among f2 primary frequency levels.
- Simple Laird and Ware (1982) linear mixed effects model with individual variances (can fit in proc mixed or R).
- Laird and Ware (1982) linear mixed effects model with common variance across all individuals (can fit in proc mixed or R).

Age-gender specific model Generalizations & simplications Conclusion

## Model comparison

The LPMLs of the six models:

	LPML
Age-gender-specific	-11785.56
Hierarchical	-11786.93
Age-gender-specific with correlation among f2	-11841.03
Hierarchical with correlation among f2	-11846.62
LMM with individual variances	-14288.11
LMM with common variance	-14723.34

Age-gender model with correlation in time and ear best. Adding correlation in frequency unnecessary and in fact adds noise. Simple mixed models perform very poorly.

Age-gender specific model Generalizations & simplications Conclusion

## Discussion

- Hierarchical & age-gender mixed models ⇒ reference charts & contour probabilities for DPOAE test-retest ototoxicity assessment.
- Allows for subject-specific correlation (i.e. smoothness) in frequency, time, and ear coupled with subject-specific linear adjustment to μ(f).
- Joint work with Junshu Bao (Duquesne); Garnett McMillan and Kristin Knight (National Center for Rehabilitative Auditory Research).