

### 7.2.3

- (a) There is significant evidence;  $p=0.085 < 0.1 = \alpha$ .
- (b) There is not significant evidence;  $p=0.065 > 0.05 = \alpha$ .

### 7.2.9

R code:

```
> normoxia=c(3.45,3.09,3.09,2.65,2.49,2.33,2.28,2.24,2.17,1.34)
> hypoxia=c(6.37,5.69,5.58,5.27,5.11,4.88,4.68,3.50)
> t.test(normoxia,hypoxia)
```

Welch Two Sample t-test

```
data: normoxia and hypoxia
t = -7.417, df = 12.212, p-value = 7.307e-06
alternative hypothesis: true difference in means is not equal to 0
```

Let  $\mu_1$  be the mean blood flow after 5 minutes of bicycle exercise of all normoxia inhalers and  $\mu_2$  be the blood flow from all hypoxia inhalers after 5 minutes of bicycle exercise. We reject  $H_0: \mu_1 = \mu_2$  at the  $\alpha = 0.05$  significance level because  $p = 0.0000073 < 0.05 = \alpha$ .

### 7.2.10

R code:

```
> d14=c(29.6,21.5,28.0,34.6,44.9)
> d15=c(32.7,40.3,23.7,25.2,24.2)
> t.test(d14,d15)
```

Welch Two Sample t-test

```
data: d14 and d15
t = 0.4943, df = 7.716, p-value = 0.6348
```

- (a) Let  $\mu_1$  be the mean weight of all chick thymus glands after 14 days incubation in mg and  $\mu_2$  be the mean weight after 15 days incubation. We accept  $H_0: \mu_1 = \mu_2$  at the  $\alpha = 0.1$  significance level because  $p = 0.63 > 0.1 = \alpha$ .
- (b) The SE of the mean difference is  $\sqrt{8.73^2/5 + 7.19^2/5} = 5.1$  mg. This is quite large relative to the actual difference 2.5 mg, so this could have easily happened by chance.

### 7.2.14

- (a)  $P = 0.03 < 0.05 = \alpha$ , we reject  $H_0$  because the p-value is less than the significance level. True.
- (b) True.
- (c) True.
- (d) True.

- (e) True. This is the definition of the p-value!  
(f) False.

### **7.2.17**

```
> control= c(3.4,1.6,4.4,2.9,3.5,2.3,2.9,2.8,2.7,2.5,2.6,2.3,3.7,1.6,  
+          2.7,1.6,2.3,3.0,2.0,2.3,1.8,3.2,2.3,2.0,2.4,2.6,2.5,2.4)  
> fertilized=c(2.8,1.9,1.9,2.7,3.6,2.3,1.2,1.8,2.4,2.7,2.2,2.6,3.6,1.3,  
+            1.2,3.0,0.9,1.4,1.5,1.2,2.4,2.6,1.7,1.8,1.4,1.7,1.8,1.5)  
> t.test(control,fertilized)
```

Welch Two Sample t-test

```
data: control and fertilized  
t = 2.9507, df = 53.503, p-value = 0.004696  
alternative hypothesis: true difference in means is not equal to 0  
95 percent confidence interval:  
 0.1739334 0.9117809
```

Let  $\mu_1$  be the mean height (cm) of all radish sprouts under control settings and  $\mu_2$  be the mean height of all radish sprouts planted in aluminum planters with fertilizer sticks. Since  $p=0.004 < 0.05=\alpha$ , we reject that there is no difference in mean height from these two populations: aluminum planters with fertilizer sticks significantly affect radish sprout growth. We are 95% confident that growth is typically increased between 0.8 and 0.9 cm under control conditions.

### **7.3.4**

The FDA approving of the drug means it is affective, i.e. the alternative  $H_A$  was chosen. The only type of error that could have occurred is Type I, rejecting  $H_0$  when it is true.

### **7.3.5**

Type II.

### **7.3.6**

The 95% CI for  $\mu_1-\mu_2$  does not include zero. We reject  $H_0: \mu_1=\mu_2$  at the 5% level.

### **7.3.7**

A 95% CI for  $\mu_1-\mu_2$  does not include zero. A 90% CI will be even smaller and centered at -4.85 (midpoint between -7.4 and -2.3), also not containing zero, therefore we reject  $H_0: \mu_1=\mu_2$  at the 10% level.

### **7.4.1**

No, association does not imply causation in an observational study. One answer might be that people with lower respiratory illnesses move

to Arizona in higher numbers to get better. Another is that many older people retire there, and they might be more prone to lower respiratory illness.

### 7.9.1

- (a) False. Either  $H_0$  is true or not (we don't know which).
- (b) True; if the p-value is less than the significance alpha, we reject.
- (c) False. If we repeat the experiment there is a 5% chance of a Type I error.
- (d) True.

### 7.9.1

```
> experimental=c(5.32,5.60,5.74,6.06,6.32,6.34,6.79,7.18)
> control=c(4.50,4.78,4.79,4.86,5.41,5.70,6.08,6.21)
> t.test(experimental,control)
```

Welch Two Sample t-test

```
data: experimental and control
t = 2.7571, df = 13.968, p-value = 0.01545
alternative hypothesis: true difference in means is not equal to 0
```

```
> t.test(experimental,control,alternative="greater")
```

Welch Two Sample t-test

```
data: experimental and control
t = 2.7571, df = 13.968, p-value = 0.007727
alternative hypothesis: true difference in means is greater than 0
```

Let  $\mu_1$  be the population mean respiration of those about to be hypnotized and  $\mu_2$  be the pop'n mean respiration of those not about to be hypnotized.

- (a) The p-value (above) is  $p=0.015$ ; we reject  $H_0: \mu_1=\mu_2$  at the 5% level and conclude  $H_A: \mu_1 \neq \mu_2$ . There is a significant difference in the mean respiration (liters/minute/ $m^2$ ) between people about to be hypnotized vs. those not about to be hypnotized.
- (b) The p-value (above) is  $p=0.008$ ; we reject  $H_0: \mu_1=\mu_2$  at the 5% level and conclude  $H_A: \mu_1 > \mu_2$ . The mean respiration (liters/minute/ $m^2$ ) among people about to be hypnotized is significantly higher than those not about to be hypnotized.
- (c) The one-sided test is appropriate for a one-sided alternative.

### 7.5.13

```
> m250=c(0.318,0.758,0.318,0.637,0.372,0.524,0.196,0.637,1.404,0.624,1.560,0.000,
+ 0.909,0.207,1.061,0.295,0.685,0.590,0.594,0.000,0.363,0.442,1.303,1.567,
+ 1.220,0.898,1.577,1.303,1.157,0.312,0.187,0.970,0.758,1.560,0.624,0.505,
```

```

+      0.849,1.592,0.909,2.411,1.019,0.362,1.705,0.829,0.329,1.019,0.884,0.909)
> m800=c(0.941,0.289,0.399,0.279,0.392,0.955,1.021,0.725,0.531,0.108,1.318,0.252,
+      0.738,0.612,1.179,0.907,0.637,0.442,0.503,0.181,0.291,0.637,0.941,0.579,
+      1.498,0.265,0.252,0.866,0.979,0.373,0.588,0.909,0.000,0.606,0.283,0.463,
+      0.490,0.337,1.248,0.163,0.813,2.010,0.277,0.000,1.213,0.293,0.544, 0.808)

```

```
> t.test(m250,m800,alternative="greater")
```

```
Welch Two Sample t-test
```

```

data: m250 and m800
t = 1.995, df = 89.843, p-value = 0.02454
alternative hypothesis: true difference in means is greater than 0

```

Let  $\mu_1$  be the settler density (juvenile fish per unit of settlement habitat) of all patch reef settlements at 250 meters from the reef crest, and  $\mu_2$  the settler density of all patch reef settlements at 800 meters from the reef crest. Since  $p=0.024 < 0.10=\alpha$ , we reject  $H_0: \mu_1=\mu_2$  in favor of  $H_A: \mu_1>\mu_2$  at the 10% significance level. That is, there is statistically significant evidence that settler density decreases as distance from the reef crest increases.

### 7.7.1

$\sigma=0.3$  cm. Jones has  $|\mu_1-\mu_2|=0.25$  cm and  $\text{power}=0.80$ ; Smith has  $|\mu_1-\mu_2|=0.5$  cm and  $\text{power}=0.95$ . The sample sizes are computed:

```

>
power.t.test(delta=0.25,sd=0.3,sig.level=0.05,power=0.80,type="two.samp
le",alternative="two.sided")

```

```
Two-sample t test power calculation
```

```

      n = 23.60472
delta = 0.25
sd = 0.3
sig.level = 0.05
power = 0.8
alternative = two.sided

```

NOTE: n is number in \*each\* group

```

>
power.t.test(delta=0.5,sd=0.3,sig.level=0.05,power=0.95,type="two.samp
le",alternative="two.sided")

```

```
Two-sample t test power calculation
```

```

      n = 10.42380
delta = 0.5
sd = 0.3
sig.level = 0.05
power = 0.95
alternative = two.sided

```

NOTE: n is number in \*each\* group

Jones needs 24 in each group; smith only needs 11.

### 7.7.3(a)

The R code for this gives 4 plants in each group; note that alternative is one-sided here:

```
>
power.t.test(delta=2,sd=0.8,sig.level=0.05,power=0.90,type="two.sample",
,alternative="one.sided")
```

Two-sample t test power calculation

```
      n = 3.678026
delta = 2
      sd = 0.8
sig.level = 0.05
      power = 0.9
alternative = one.sided
```

NOTE: n is number in \*each\* group

### 7.10.3

```
> toluene=c(3420,2314,1911,2464,2781,2803)
> control=c(1820,1843,1397,1803,2539,1990)
> wilcox.test(toluene,control)
```

Wilcoxon rank sum test

```
data: toluene and control
W = 32, p-value = 0.02597
alternative hypothesis: true location shift is not equal to 0
```

(a) Since  $p=0.026 < 0.05 = \alpha$ , we reject  $H_0$ : the population distributions of dopamine from toluene and control populations are the same at the 5% significance level and conclude that they are different.

```
> wilcox.test(toluene,control,alternative="greater")
```

Wilcoxon rank sum test

```
data: toluene and control
W = 32, p-value = 0.01299
alternative hypothesis: true location shift is greater than 0
```

(b) Since  $p=0.013 < 0.05 = \alpha$ , we reject  $H_0$ : the population distributions of dopamine from toluene and control populations are the same at the 5% significance level and conclude that dopamine tends to be higher in toluene-exposed rats.

### 7.10.3

```
> joggers=c(39,40,32,60,19,52,41,32,13,37,28)
> program=c(70,47,54,27,31,42,37,41,9,18,33,23,49,41,59)
> wilcox.test(joggers,program)
```

Wilcoxon rank sum test with continuity correction

data: joggers and program

W = 71.5, p-value = 0.5854

alternative hypothesis: true location shift is not equal to 0

Warning message:

In wilcox.test.default(joggers, program) :

cannot compute exact p-value with ties

Ignore the "ties" warning. Since  $p=0.58 > 0.1 = \alpha$ , there is not statistically significant evidence that distributions of HBE differ between joggers and fitness program entrants (at the 10% significance level).