

## Good and Bad Graphs

- ***Example 1:*** Look at the graph comparing the interest rates of several lenders.
- **What is the perception that the reader has initially?**
- **How well or poorly does this perception reflect the truth of the numerical comparison?**

## Types of Data

- ***Categorical Variables*** place individuals into one of several categories.
- ***Quantitative or (Numerical) Variables*** measure a characteristic of an individual with a (mathematically meaningful) number.
- It makes sense to add, or average, the values of a numerical variable.
- Variables measured on college applicants: SAT score, high school GPA, race, gender, number of AP courses taken.
- Which are categorical? Which are quantitative? (Clicker quiz next)

## Clicker Quiz 1

**Variables measured on college applicants: SAT score, high school GPA, race, gender, number of AP courses taken.**

**Which are categorical? Which are quantitative?**

**A. *Categorical:* race, gender, number of AP courses taken.**

***Quantitative:* SAT score, high school GPA.**

**B. *Categorical:* gender. *Quantitative:* race, SAT score, high school GPA, number of AP courses taken.**

**C. *Categorical:* race, gender, high school GPA. *Quantitative:* SAT score, number of AP courses taken.**

**D. *Categorical:* race, gender. *Quantitative:* SAT score, high school GPA, number of AP courses taken.**

## Data Tables

- A *data table* is often a reasonable way to summarize data, especially categorical data.
- A table is a non-graphical way to present the *distribution* of a variable.
- The *distribution* of a variable indicates two things: (1) What value(s) a variable can take, and (2) how often it takes those values.
- A value's *frequency* is a count of how many times it has occurred in a data set.
- A value's *relative frequency* is the proportion of times it has occurred in a data set.

## An Example Data Table

Table 1: Counts for students in an introductory statistics class, Summer 2002.

<b>Year in School</b>	<b>Count</b>	<b>Percent</b>
<b>Freshman</b>	<b>18</b>	<b>41.9%</b>
<b>Sophomore</b>	<b>10</b>	<b>23.3%</b>
<b>Junior</b>	<b>6</b>	<b>14.0%</b>
<b>Senior</b>	<b>9</b>	<b>20.9%</b>
<b>Total</b>	<b>43</b>	<b>100%</b>

## Rates vs. Counts (Again)

- Previous table presents the *distribution* of the variable “Year in School.”
- Note that *rates* may be more useful/informative in a data table than raw counts.
- Especially true when there are a huge number of individuals in the overall data set.
- When percentages in a table are rounded off, total percentage may not add to 100% due to *roundoff error*.
- Check previous table:  $41.9 + 23.3 + 14.0 + 20.9 = ?$

## Pie Charts and Bar Graphs

- ***Pie Charts* and *Bar Graphs* are common ways to present a graphical summary of *categorical* data.**
- ***Pie Charts* present proportions as wedges in a circle of various sizes.**
- **Visually we immediately see “pieces of a whole.”**
- ***Bar graphs* present proportions as vertical bars of various heights.**
- **Easy to immediately compare categories to see which is biggest, smallest, etc.**
- **See example *Pie Chart* and *Bar Graph* for school-year data.**

## Notes and Cautions: Pie Charts and Bar Graphs

- ***Pie Charts* and *Bar Graphs* are not appropriate for summarizing *quantitative* data (unless we define certain numerical classes for the data).**
- ***Bar Graphs* are easier to construct by hand than *Pie Charts*.**
- **These types of graphs are usually generated with the help of software.**
- ***Bar Graphs* can also graph data that are not part of a whole (see example with Tax Data for Countries).**



## More on Pie Charts and Bar Graphs

- **From the help file of a statistical software package: “Pie charts are a very bad way of displaying information. The eye is good at judging linear measures and bad at judging relative areas.”**
- **Based on empirical investigations of Cleveland (1985) and McGill as well as investigations by perceptual psychologists.**
- **Make sure the numerical axis of the bar graph is not misleading (recall Example 1!).**

## Clicker Quiz 2

**What type of variable's distribution could most easily be represented by a pie chart or bar graph?**

- A. Height of basketball players**
- B. 100-meter dash time of sprinters**
- C. Party of members of Congress**
- D. Weight of oranges**

## Pictograms and their Drawbacks

- ***Pictograms* are like *Bar Graphs*, but use a picture rather than a simple bar to represent proportions.**
- **The width of the picture is often increased with the height so the pictures aren't distorted.**
- **Our eye perceives the whole area of the picture, rather than just the height.**
- **This makes comparing categories quite deceptive.**
- **See example showing building permit data.**

## Line Graphs

- ***Line Graphs* show the pattern of variation of some variable *over time*.**
- **Time (in years? months? days? hours?) is always plotted on the horizontal axis.**
- **The value of the variable is plotted on the vertical axis.**
- **Look for *overall pattern*: Increasing trend? Decreasing trend? Constant trend?**
- **Look for times when the pattern shows *deviation* from the overall trend.**
- **Look for *seasonal variation*, especially common when data are plotted monthly or weekly (gas prices example).**
- **See example showing freshman percentage over several years.**

## Clicker Quiz 3

**If we plotted the annual proportion (over a couple of decades) of eligible citizens who voted on Election Day, what type of pattern would we likely see?**

- A. Seasonal variation**
- B. Increasing trend**
- C. Decreasing trend**
- D. Completely haphazard variation**

## More on Line Graphs

- **Advanced statistical methods can adjust for (remove) seasonal variation from data.**
- **If a variable is known vary seasonally, it's more instructive to study the pattern *after removing* the seasonal variation.**
- ***Example:* Unemployment rate known to always rise in January. Why?**
- **Very important to use the *appropriate scales* for the axes.**
- **The appearance of line graphs can change greatly if the scales are changed.**
- **Could lead to deceptive conclusions.**
- **See Example: Data on unmarried couples.**

## Clicker Quiz 4

**What is another aspect of the unmarried couples plot that could use improvement?**

- A. A different color should be used for each decade (1980s, 1990s, etc.)**
- B. Couples (rather than thousands of couples) should be plotted on the vertical axis.**
- C. Instead of the count of unmarried couples being plotted, a rate should be used to account for population changes.**

## **More Graphs: Good, Not-so-good, Terrible**

- **Compare the two graphs (on page 204 of book) showing stock performances from 1970-2003**
- **What is top graph showing? What is bottom graph showing?**
- **Which shows the pattern of variation of stock prices better?**
- **Another Example: State and Local Property Taxes Graph**
- **How would you change the scales on these axes?**



## Good Graphical Practices

- Use *labels* and *legends* to say what variables are plotted, units, source of data, etc.
- Make the data stand out, not fancy artistic flourishes.
- Have the information reflect what the eye initially sees.
- Avoid cluttering the plot with needless visual elements.
- Be wary of misleading graphs that you may encounter!