STAT588/BIOL588: Genomic Data Science Lecture 15: Differential Expression Analysis

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Objectives of Lecture 15

- ► Simple Differential Expression
- ► Advanced Differential Expression



Borrowing Strength

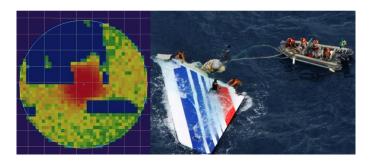
- An advantage of having tens of thousands of genes is that we can try to learn about typical standard deviations by looking at all genes
- ▶ Empirical Bayes gives us a formal way of doing it



Air France 447



Bayesian Inference



- During the search for Air France 447, from 2009-2011, knowledge about the black box location was described via Bayesian inference.
- Eventually, the black box was found in the red area.
- Searching for a fisherman lost at sea

 $https://www.nytimes.com/2014/01/05/magazine/a-speck-in-the-sea.html?_r{=}1$

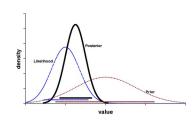
Bayesian Approach

$$egin{array}{lll} heta & \sim & G \ Y| heta & \sim & f(y| heta) \end{array}$$

- G is the prior
- f is the sampling distribution

Posterior Distribution

$$g(\theta|Y) = \frac{f(y|\theta)g(\theta)}{f_G(Y)}$$



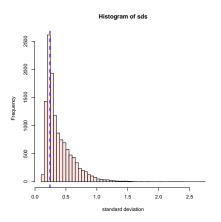
Marginal Distribution

$$f_G(Y) = \int f(y|u)g(u)du$$



Shrinkage Estimate

$$ilde{s}_g^2 = rac{s_g^2 d_g + s_0^2 d_0}{d_g + d_0}, \quad ilde{t}_g = rac{\hat{eta}_g}{ ilde{s}_g \sqrt{c_g}}$$





Posterior Statistics: eBayes and SAM

Posterior variance estimators

$$\tilde{s}_g^2 = \frac{s_g^2 d_g + s_0^2 d_0}{d_g + d_0}$$

Moderated t-statistics

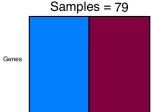
$$ilde{t}_g = rac{\hat{eta}_g}{ ilde{\mathsf{s}}_g \sqrt{\mathsf{c}_g}}$$

Eliminates large t-statistics merely from very small sd



Advanced Differential Expression

```
Y = \beta_0 + \beta_1 \times \text{BCR/ABL} >library("limma")
 >design = cbind(mean = 1, diff = cl)
 >design[1:5,]
 >fit = lmFit(exprs(ALLset1), design)
 >fit = eBayes(fit)
 >topTable(fit, coef=2)
```





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Top Table

	ID	logFC	AveExpr	t	P.Value	adj.P.Val	В
156	1636_g_at	1.10	9.20	9.03	4.88e-14	1.23e-10	21.29
1915	39730_at	1.15	9.00	8.59	3.88e-13	4.89e-10	19.34
155	1635_at	1.20	7.90	7.34	1.23e-10	1.03e-07	13.91
163	1674_at	1.43	5.00	7.05	4.55e-10	2.87e-07	12.67
2066	40504_at	1.18	4.24	6.66	2.57e-09	1.30e-06	11.03
2014	40202_at	1.78	8.62	6.39	8.62e-09	3.63e-06	9.89
1262	37015_at	1.03	4.33	6.24	1.66e-08	6.00e-06	9.27
437	32434_at	1.68	4.47	5.97	5.38e-08	1.70e-05	8.16
1269	37027_at	1.35	8.44	5.81	1.10e-07	3.08e-05	7.49
1366	37403_at	1.12	5.09	5.48	4.27e-07	1.08e-04	6.21



Annotation

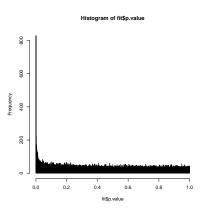
```
>library("hgu95av2.db")
>ALLset1Syms = unlist(mget(featureNames(ALLset1), env
= hgu95av2SYMBOL))
>topTable(fit, coef = "diff", adjust.method = "fdr",
sort.by = "p", genelist = ALLset1Syms)
>plot(-log10(tt$p.value), -log10(fit$p.value[,
"diff"]), xlab = "-log10(p) from two-sample t-test",
ylab = "-log10(p) from moderated t-test (limma)",
pch=".")
>abline(c(0, 1), col = "red")
```

Top Table

	ID	logFC	AveExpr	t	P.Value	adj.P.Val	В
156	ABL1	1.10	9.20	9.03	4.88e-14	1.23e-10	21.29
1915	ABL1	1.15	9.00	8.59	3.88e-13	4.89e-10	19.34
155	ABL1	1.20	7.90	7.34	1.23e-10	1.03e-07	13.91
163	YES1	1.43	5.00	7.05	4.55e-10	2.87e-07	12.67
2066	PON2	1.18	4.24	6.66	2.57e-09	1.30e-06	11.03
2014	KLF9	1.78	8.62	6.39	8.62e-09	3.63e-06	9.89
1262	ALDH1A1	1.03	4.33	6.24	1.66e-08	6.00e-06	9.27
437	MARCKS	1.68	4.47	5.97	5.38e-08	1.70e-05	8.16
1269	AHNAK	1.35	8.44	5.81	1.10e-07	3.08e-05	7.49
1366	ANXA1	1.12	5.09	5.48	4.27e-07	1.08e-04	6.21



P values

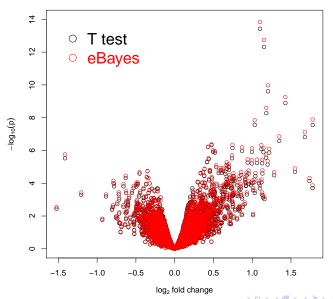


A p value of 0.05 implies that 5% of all the tests will result in false positives.

A FDR adjusted p value (or q value) of 0.05 implies that 5% of significant tests can be false positives.



Volcano Plot



Summary

- When sample size is small, sd estimates are unstable and t-test is less powerful.
- ▶ eBayes and SAM provide more powerful moderate t-statistics which borrow strength from all genes.

