## Homework 02

STAT 509 Statistics for Engineers<br>Summer 2017 Section 001<br>Instructor: Tahmidul Islam

## Question 01

$A$ and $B$ are two events in the sample space $S$. Assume $P(A)=0.25$ and $P(B)=0.4$ and $P(A \cup B)=0.6$. Calculate the following probabilities. Clearly state what probability rules you used. (Hint: You can draw Venn Diagrams to help you visualize the relationship among two events and the sample space.)
a $P(\bar{A})$.
b $P(A \cap B)$.
c $P(\bar{A} \cup \bar{B})$.
d $P(B \mid A)$.
e Are A and B are independent events? Why or why not?

## Question 02

Transactions to a computer database are either new items or changes to previous items. The addition of an item can be completed in less than 100 milliseconds $90 \%$ of the time, but only $20 \%$ of changes to a previous item can be completed in less than this time. If $30 \%$ of transactions are changes, what is the probability that a transaction can be completed in less than 100 milliseconds? (Try to draw a tree diagram).

## Question 03

The probability that a randomly chosen automobile will need an oil change is 0.25 ; the probability that it needs a new oil filter is 0.40 ; and the probability that both the oil and filter need changing is 0.14 .
a What is the probability that a car will need an oil change or new filter?
b If the oil had to be changed, what is the probability that a new oil filter is needed?
c If a new oil filter is needed, what is the probability that the oil has to be changed?
d Are oil filter and needing an oil change independent of one another. Why?

