

## STAT 509 2017 Summer HW11

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Lecture Day: May 25

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1. In a random sample of 85 automobile engine crankshaft bearings, 7 have a surface finish roughness that exceeds the specifications. Does this data present sufficient evidence that the proportion of crankshaft bearings, say  $p$ , exhibiting excess surface roughness is greater than 0.06? We will address this using a hypothesis test.
  - (a) State the null and alternative hypotheses.
  - (b) Calculate the appropriate test statistic.
  - (c) What is the  $p$ -value of the test?
  - (d) What is your conclusion based on the  $p$ -value if we use  $\alpha = 0.1$ ?
  - (e) Calculate a 90% confidence interval for the population proportion. Interpret the confidence interval using the context of the question.
  - (f) Compare the results in (d) and (e), are they similar?
  - (g) What is the probability to make type I error?
2. You plan to hold a party for your friends, and you are interested to know at 95% confidence level, whether less than 60% of students will attend. Denote  $p$  to be the true percentage of students who will show up. We have

$$H_0 : p = 0.6$$

$$H_a : p < 0.6$$

- (a) What is the type I error here? What is the potential consequence for type I error?
- (b) What is the type II error here? What is the potential consequence for type II error?