

STAT 509 2017 Summer HW17

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Lecture Day: June 13

1. Matrix A and vector B is defined respectively by

$$A = \begin{pmatrix} 3 & 7 \\ 12 & -2 \end{pmatrix}, B = \begin{pmatrix} 4 \\ 9 \end{pmatrix}$$

- (a) Calculate AB
 - (b) Calculate A^T
 - (c) Calculate $A^T B$
 - (d) Calculate $B^T A^T$
2. In `gala` dataset, suppose we want to form a multiple linear regression model using `Species` as response, and all others as predictors (independent variables). Represent the model using matrix notation \mathbf{Y} , \mathbf{X} , β , and ϵ , and mark the dimension for each vector and matrix. (*Hint: Slides page 10*)
3. There are two matrices A and B , defined by

$$A = \begin{pmatrix} 2 & 1 \\ 4 & -2 \end{pmatrix}, B = \begin{pmatrix} 0.25 & 0.125 \\ 0.5 & -0.25 \end{pmatrix}$$

- (a) Calculate AB
- (b) Calculate BA
- (c) Do you find that the two results in (a) and (b) are the same? The result is called identity matrix. For any matrix M , the inverse matrix of M can be wrote as M^{-1} , and by definition of inverse matrix, $MM^{-1} = M^{-1}M = I$, where I is the identity matrix. Using the previous results to find A^{-1} and B^{-1} .