

Midterm Exam

1. Consider the following 2X2 table with fixed row and column marginals:

12	3	15
3	7	10
15	10	25

- (a) What is the range of n_{11} ?
- (b) Consider the exact test of $H_o : \theta = 2$ vs. $H_A : \theta > 2$ ($\alpha = .05$). Find the rejection region and compute a p-value for this test.
2. Use the function `pexact` to help answer the following questions about unconditional tests for the 2x2 table below.

3	7	10
8	2	10
11	9	20

Assume that the row marginals, n_{1+}, n_{2+} are fixed, so that n_{i1} has a binomial distribution with parameters n_{i+} and π_i .

- (a) Which tables lie in the pooled Z-test rejection region for the hypothesis $H_o : \pi_1 = \pi_2$ vs. $H_a : \pi_1 < \pi_2$? Answer this by entering an arbitrary value for π when using `pexact` and then examining the output list.
- (b) The following set of commands can generate a vector of p-values for a range of π :
- ```

p=rep(0,100)
pv=rep(0,100)
for (i in 1:100) {
p[i]=i/101
pv[i]=pexact(p[i],3,7,8,2)$pval
}

```
- Plot the p-value for the test as a function of  $\pi$ ,  $0 \leq \pi \leq 1$ . What is its sup?
- (c) Now construct a Clopper-Pearson 99.9% CI for  $\pi$  (You can use Berger's web page for this). Would the p-value computed over the Clopper-Pearson CI range be any different from the p-value computed over the entire range of  $\pi$ ? Why or why not?
3. The table below was compiled for a middle school from the 2003 English/Language Arts PACT exam.

|             | Grade |     |     |
|-------------|-------|-----|-----|
|             | 6     | 7   | 8   |
| Below Basic | 60    | 62  | 76  |
| Basic       | 87    | 134 | 140 |
| Proficient  | 87    | 102 | 100 |
| Advanced    | 42    | 24  | 21  |

- (a) Compute the likelihood ratio test statistic for a test of independence
- (b) Partition the likelihood ratio test statistic into 6 independent 1 df components. What conclusions can you draw from these components?