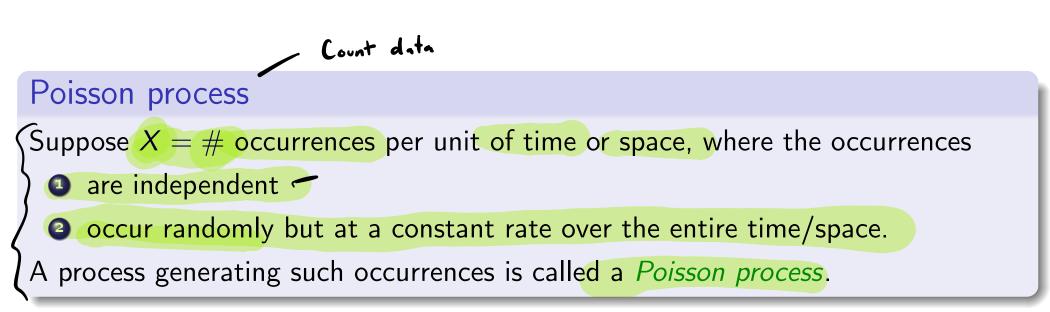


These slides are an instructional aid; their sole purpose is to display, during the lecture, definitions, plots, results, etc. which take too much time to write by hand on the blackboard. They are not intended to explain or expound on any material.

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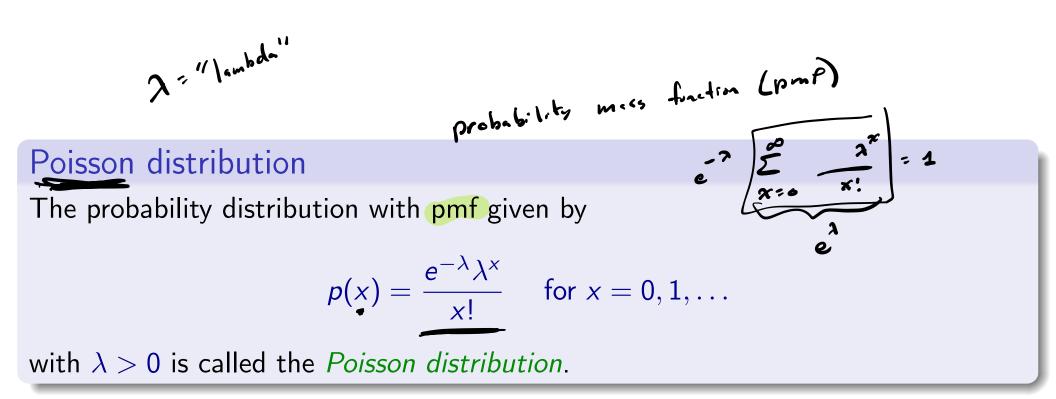


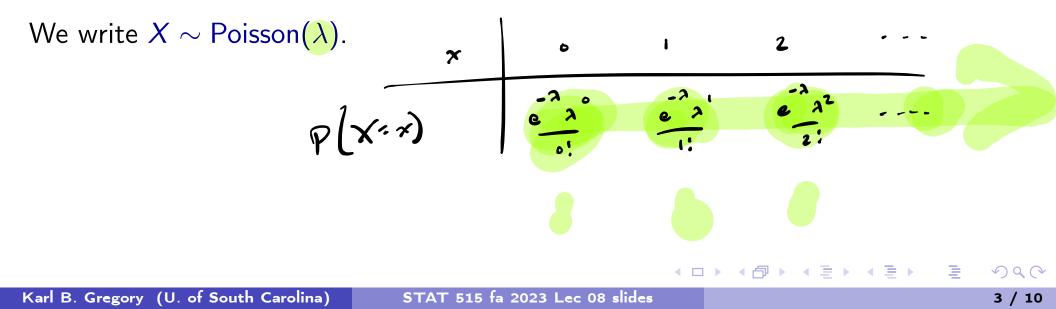
Examples:

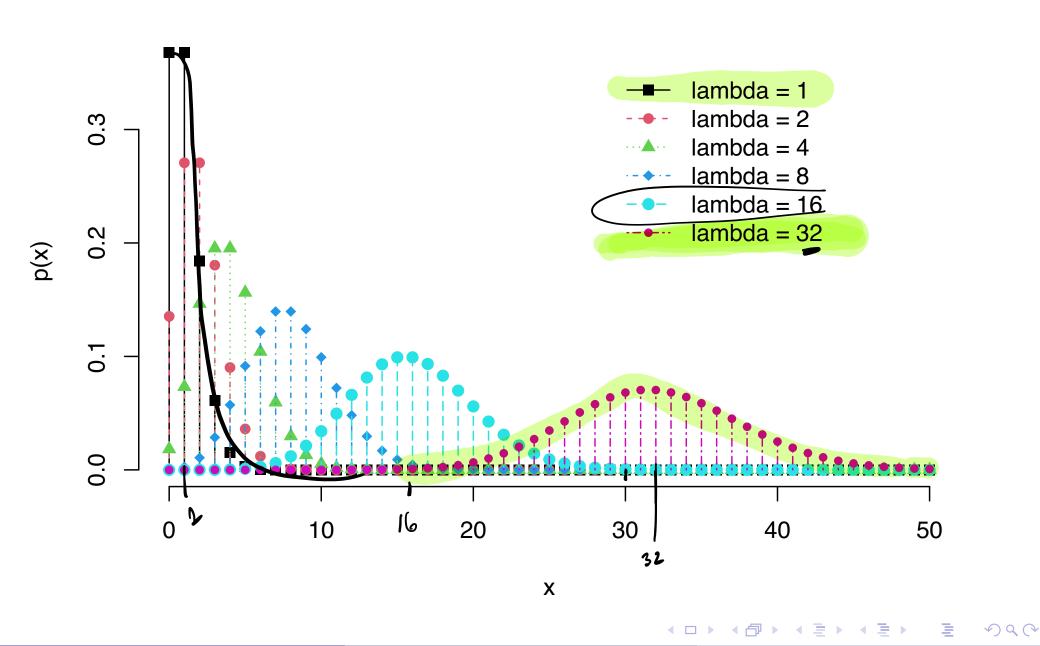
- # customers entering a store in an hour.
- # earthquakes per decade in a region.
- \bigcirc # weeds growing per square meter of a field.
- # bird nests per acre in a habitat.

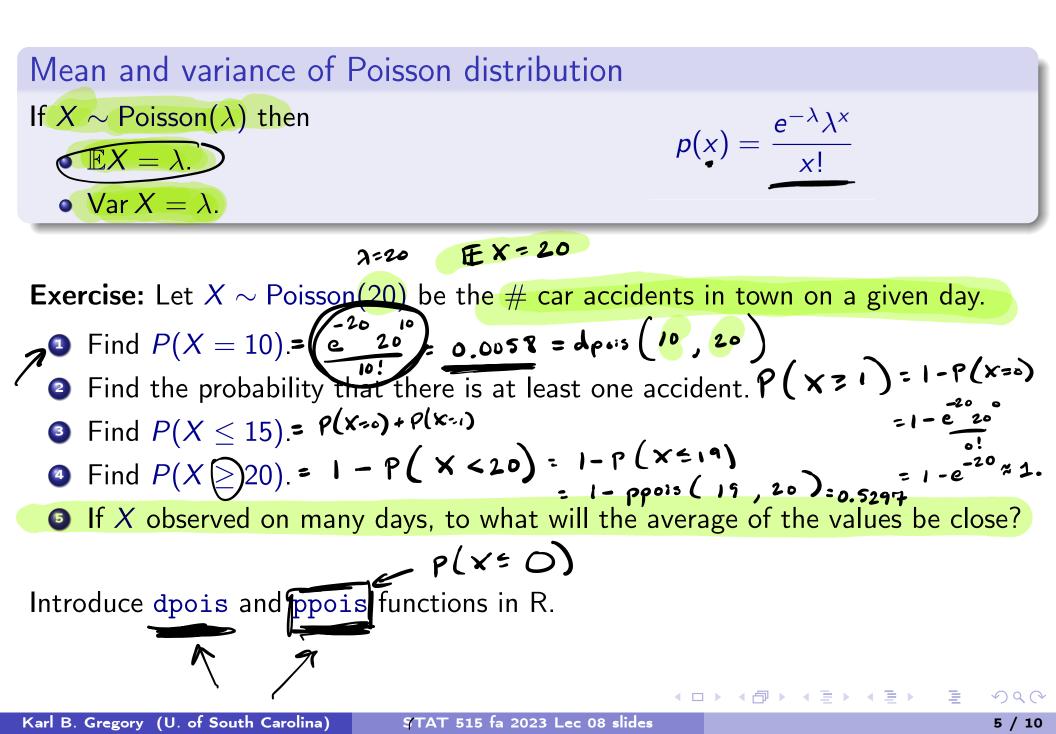


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$$S(3) P(X = 15) = P(X = 0) + P(X = 1) + ... + P(X = 15)$$

$$T = \frac{20}{0!} \frac{20}{0!} + \frac{20}{1!} \frac{1}{1!} + \frac{20}{15!} \frac{20}{15!}$$

$$T = \frac{20}{15!} \frac{20}{1!} \frac{1}{1!}$$

$$T = \frac{20}{15!} \frac{20}{1!} \frac{1}{1!}$$

$$T = \frac{20}{15!} \frac{20}{1!} \frac{1}{1!}$$

$$T = \frac{20}{15!} \frac{1}{1!}$$

= 0.1565

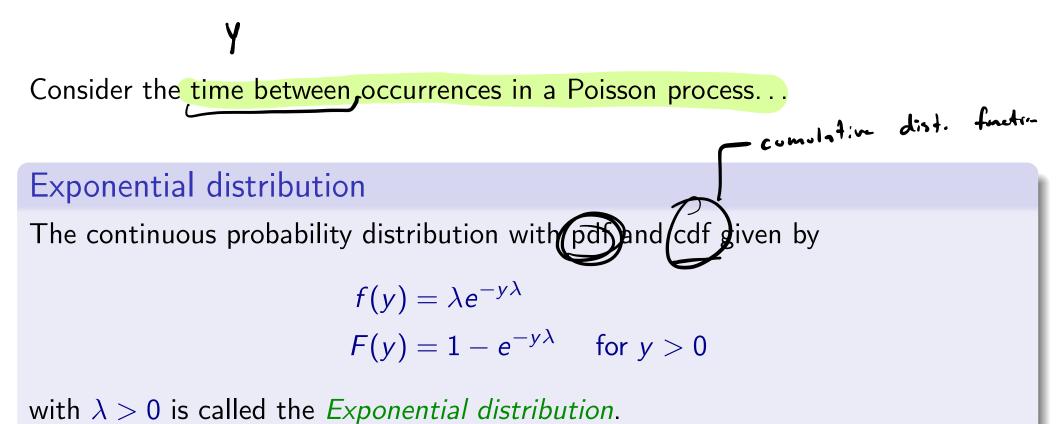
$$p(x) = \frac{e^{-\lambda} x}{\underbrace{\otimes}}$$

Mean number of occurrences scales with unit of time/space...

Let
$$X \sim \text{Poisson}(\lambda)$$
, where $X = \#$ occurrences per unit time/space of an event.
Then if $Y = \#$ occurrences in t units of time/space, we have $Y \sim \text{Poisson}(t\lambda)$.
 $X \sim \text{Poisson}(2\circ)$, $\#$ occidents in 4 div_{X} .
Exercise: Let Y be the $\#$ car accidents in town in a given week.
 $0 \text{ What is the distribution of } Y$? Refer to previous example.
 4 div_{X} .
 $9 \text{ Find } P(Y \le 130) = \frac{P^{0.13}(130}{140}, 140) = 0.2124$
 $9 \text{ Find } P(Y = 140) = e^{-140} 140^{140} = 40^{110} (140, 140) = 0.0337$
 $9 \text{ t} = 4$
 $9 \text{ Find } P(Y \ge 150)$.
 $= 7 \text{ Y} \sim \text{Poisson}(4.2\circ)$
 140

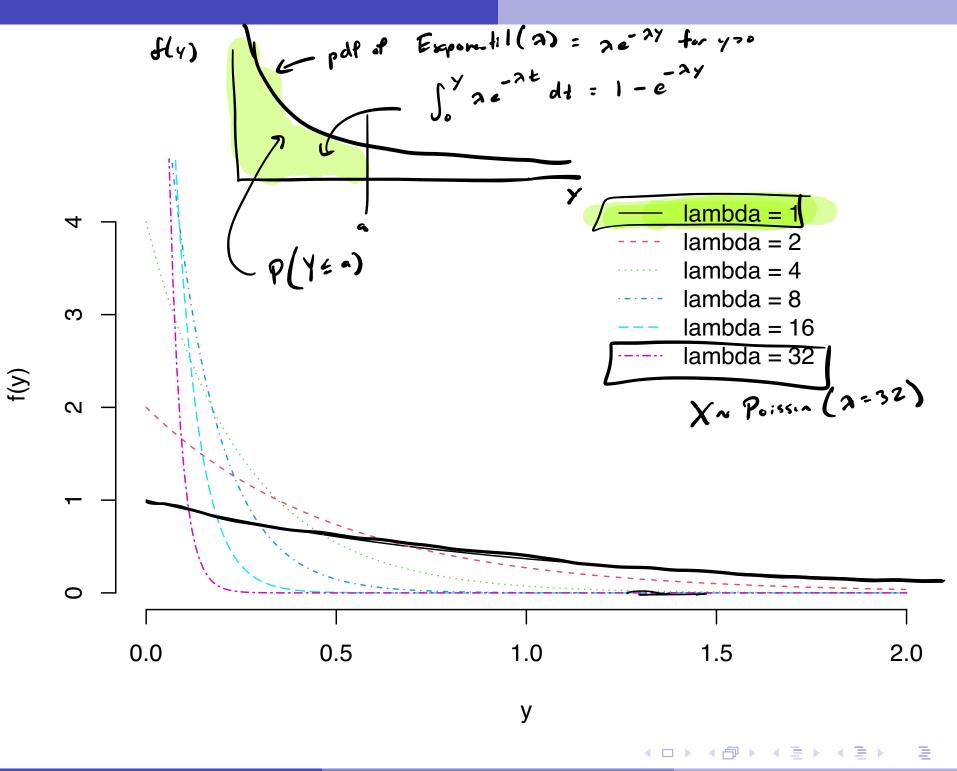
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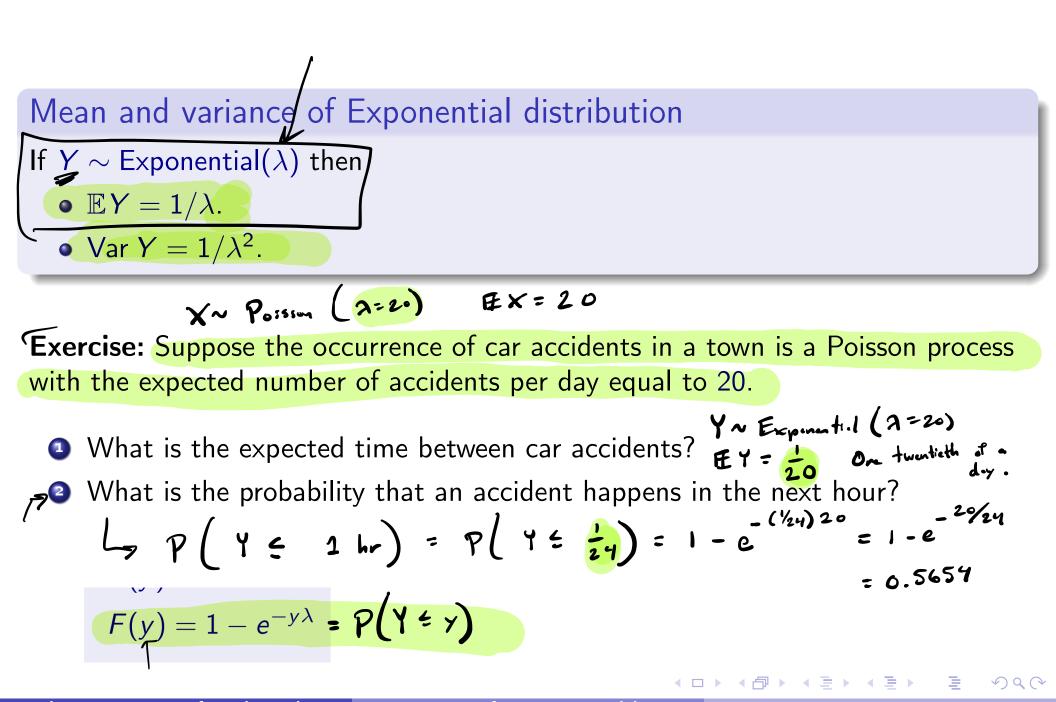


We write $Y \sim \text{Exponential}(\lambda)$.

Derive: Start with P(Y > y) = P(no occurrences before time y).



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Exercise: Suppose the occurrence of blown-out tires along a freeway is a Poisson process with the expected number of blown-out tires per mile equal to 1/3.

Find the probabilities of the following:

1 finding 2 blown-out tires in the next mile.
$$P(X=2) = e_{\frac{1}{2}} \left(\frac{1}{2} \right)^{2} = de^{-is} \left(2, \frac{1}{3} \right)^{3}$$

2 finding at least one blown-out tire in the next mile. $= 0.0398$
3 find 2 blown-out tires in the next 12 miles. $W \sim P_{0:sson} \left(x = 12 \cdot \frac{1}{3} = 4 \right)$

finding fewer than 3 blown-out tires in the next 12 miles.

- finding a blown-out tire exactly 5 miles down the road.
- finding a blown-out tire before going further than 5 miles.

not finding a blown-out tire in the next 3 miles.

$$2 P(X = 1) = 1 - P(X = 0) = 1 - \frac{e^{-y_3}}{y_3} = 1 - e^{-y_3}$$
$$= 1 - \frac{1}{2} P(X = 1) = 1 - \frac{1}{2} P(X = 0) = \frac{1}{2} P($$

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(3)
$$P(W=2) = \frac{-4}{2!} \frac{1}{2!} = dp_{0}ii(2, 4)$$

(4) $P(W=3) = P(W=2) = pp_{0}ii(2, 4) = 0.238$
(5) $P(Y=5) = I - e^{-5(\frac{1}{3})} = I - e^{-\frac{5}{3}}$
 $P(Y=5) = I - e^{-\frac{5}{3}} = I - e^{-\frac{5}{3}}$

