STAT 515 fa 2023 Lec 13 slides

Sample size calculations

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These slides are an instructional aid; their sole purpose is to display, during the lecture, definitions, plots, results, etc. which take too much time to write by hand on the blackboard. They are not intended to explain or expound on any material.

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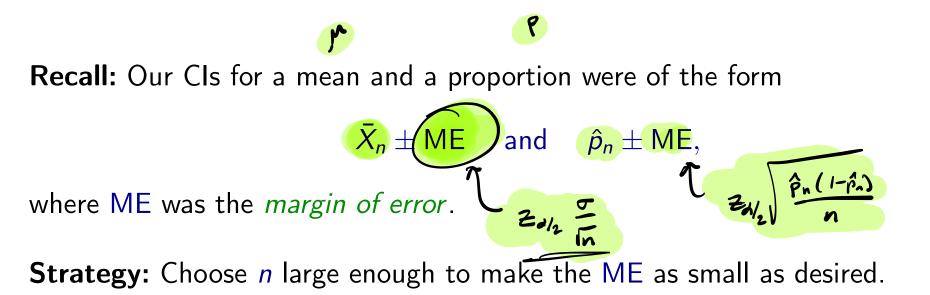
How to choose the sample size *n*?

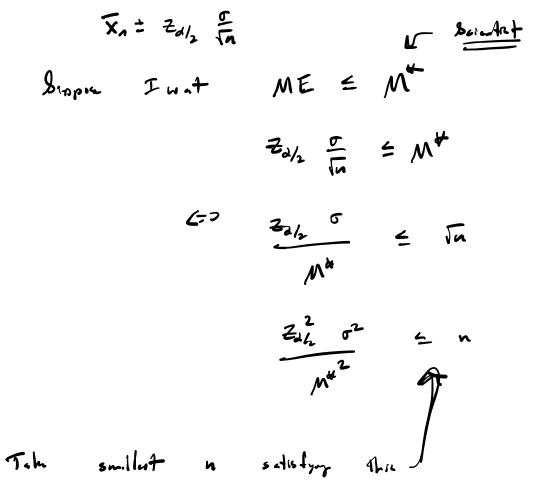
Two questions for determining sample size	
How narrow do we want confidence intervals to be?	
What level of confidence do we want to have?	95%

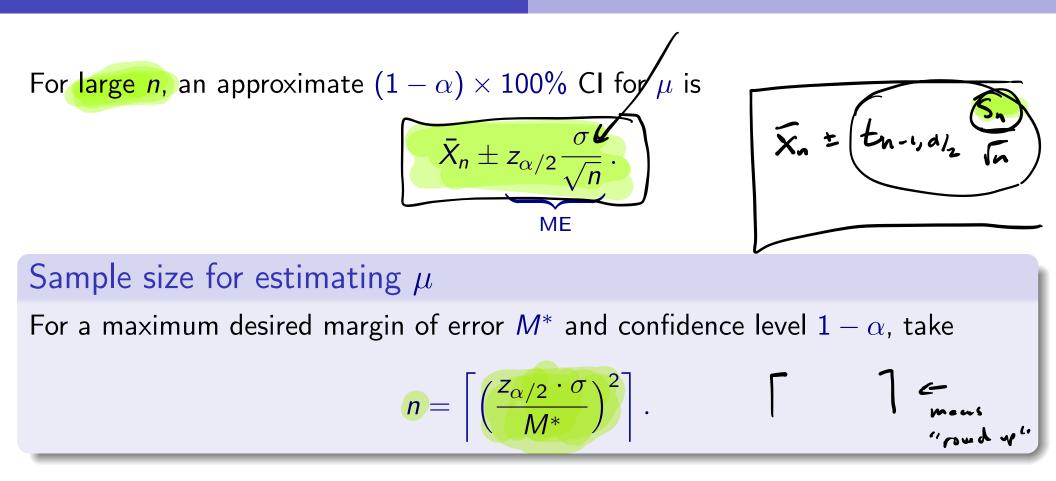


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In the above, $\lceil x \rceil$ is the smallest integer greater than or equal to x ("round up").

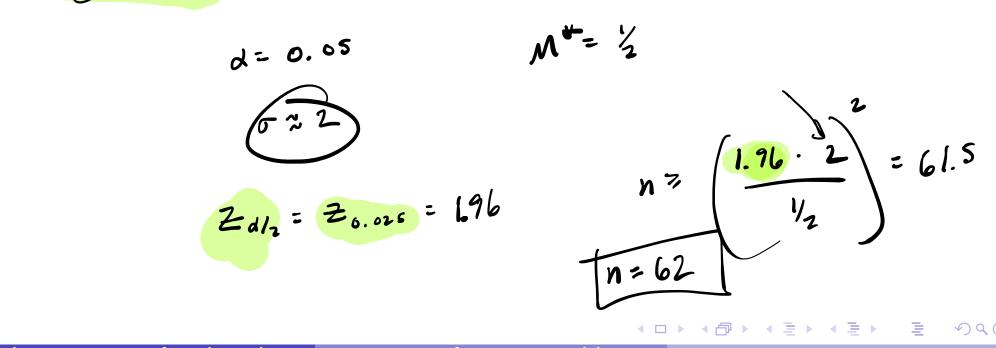
The unknown σ can be replaced by an estimate from a previous or pilot study.

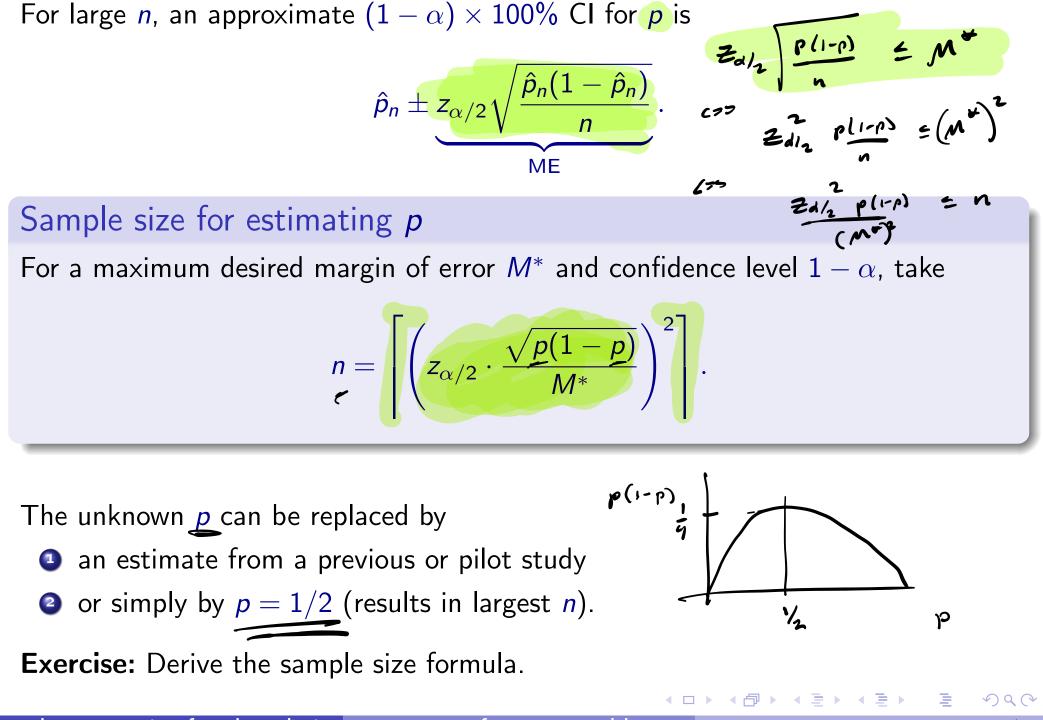
Exercise: Derive the sample size formula.

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$$n \neq \left(\frac{z_{d/2} \cdot \sigma}{M^*}\right)^2$$

Exercise: Researchers wish to estimate the mean gestation period of tortoises with the margin of error at the 95% confidence level no greater than 0.5 months. Previous studies have estimated the standard deviation of gestation periods to be roughly 2 months. What sample size should be used?





$$n = \left(\frac{Z_{A/2} \sqrt{p(1-p)}}{\Lambda^*} \right)^2$$

Exercise: We wish to estimate with <u>99%</u> confidence the proportion of voters who will vote for a particular candidate with a ME no greater than <u>2 percentage</u> points. What sample size do we need?

$$A = 0.01 , \quad Z_{d/2} = Z_{.005} = 2.5758$$

$$M^{+} = 0.02$$

$$N = \left(\frac{2.5758 \cdot \sqrt{2}(1-\frac{1}{2})}{0.02}\right) = \left(\frac{2.5758 \cdot \frac{1}{2}}{0.02}\right)$$

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= 4,146.7

$$\left(\frac{1.76 \cdot \frac{1}{2}}{.02}\right)^2 = 2,401.$$