

Formula Sheet – Final Exam – SCCC 312A

Classical (Wald)  $1 - \alpha$  CI for  $p$ :

$$\left( \hat{p} - z(\alpha/2) \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}, \hat{p} + z(\alpha/2) \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}} \right)$$

Agresti-Coull  $1 - \alpha$  CI for  $p$ :

$$\left( \tilde{p} - z(\alpha/2) \sqrt{\frac{\tilde{p}(1 - \tilde{p})}{\tilde{n}}}, \tilde{p} + z(\alpha/2) \sqrt{\frac{\tilde{p}(1 - \tilde{p})}{\tilde{n}}} \right)$$

where  $\tilde{n} = n + [z(\alpha/2)]^2$  and  $\tilde{p} = \frac{x + 0.5[z(\alpha/2)]^2}{\tilde{n}}$ .

$1 - \alpha$  CI for  $\mu$ :

$$\left( \bar{x} - t(n - 1, \alpha/2) \frac{s}{\sqrt{n}}, \bar{x} + t(n - 1, \alpha/2) \frac{s}{\sqrt{n}} \right)$$

Test statistic (hypothesis test about  $\mu$ ):

$$t^* = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$$

CI and test statistics for  $\mu_d$  in paired-sample  $t$ -test: Same as above but with  $\bar{x}_d$  and  $s_d$ .

Test statistic (hypothesis test about  $p$ ):

$$z^* = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$$

$1 - \alpha$  CI for  $\mu_1 - \mu_2$ :

$$\left( (\bar{x}_1 - \bar{x}_2) - t(df, \alpha/2) \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}, (\bar{x}_1 - \bar{x}_2) + t(df, \alpha/2) \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} \right)$$

Test statistic (comparing two means, independent samples):

$$t^* = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

$1 - \alpha$  CI for  $p_1 - p_2$ :

$$\left( (\hat{p}_1 - \hat{p}_2) - z(\alpha/2) \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}}, (\hat{p}_1 - \hat{p}_2) + z(\alpha/2) \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}} \right)$$

Test statistic (comparing two proportions):

$$z^* = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}(1 - \hat{p}) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

where  $\hat{p}$  is the pooled sample proportion.