Bayesian Logistic Regression

- The logistic regression approach does not assume the unobserved latent variable is normally distributed.
- We define Y to be either 1 (success) or 0 (failure) and model P(Y = 1) at a given value x of the explanatory variable X as:

$$\pi_x = \frac{e^{\beta_0 + \beta_1 x}}{1 + e^{\beta_0 + \beta_1 x}}$$

where $\pi_{x} = P(Y = 1 | X = x)$.

This is equivalent to modeling the log-odds of success with a linear predictor function:

$$logit(\pi_x) = ln\left(rac{\pi_x}{1-\pi_x}
ight) = eta_0 + eta_1 x$$

- A common choice is choosing normal priors on the regression coefficients (β₀ and β₁).
- Alternately, we could specify beta priors on the success probabilities at selected x-values of interest.
- We could then express the β's deterministically in terms of those success probabilities by back-solving.
- See WinBUGS examples on course web page with senility data.