

### Stat509 Fall 2014 HW3

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**Instruction:** Please finish this homework before the class on 10/07. You will have a quiz based on the homework during the class.

1. In 1990 the lead concentration in gasoline ranged from 0.1 to 0.5 grams/liter. Let  $Y$  = grams per liter of lead in gasoline. The probability density function for  $Y$  is

$$f(y) = 12.5y - 1.25, \text{ for } 0.1 < y < 0.5.$$

- (a) What is the probability that a random liter of gasoline would contain between 0.1 and 0.4 grams/liter of lead?
  - (b) What is the probability that a random liter of gasoline will contain more than 0.3 grams/liter of lead?
  - (c) Give the cumulative probability function  $F_Y(y)$  (*Hint: you need to discuss the value of  $y$  by cases*).
  - (d) Use the cumulative probability function  $F_Y(y)$  to calculate the probability that a random liter of gasoline will contain less than 0.35 grams of lead.
  - (e) Calculate the expected value of  $Y$ .
  - (f) Calculate the variance for  $Y$ .
2. Explosive devices used in mining operations produce (nearly) circular craters when detonated. The radii of these craters, say,  $Y$ , follow an exponential distribution with  $\lambda = 0.10$ .
    - (a) Find the proportion of radii that will exceed 20 meters.
    - (b) Find the probability that a single denotation will produce a radius between 5 and 15 meters.
    - (c) The area of the crater is  $W = \pi Y^2$ . Find the expected (mean) area produced by the explosive devices; that is, compute  $E(W)$ .
  3. Suppose  $X$  has an exponential distribution with a mean of 10. Calculate  $P(X < 15 | X > 10)$ . (*Hint: apply the memoryless property*)
  4. The number of calls received by a telephone answering service follows a Poisson distribution. The calls average 20 per hour.
    - (a) What is the probability that 30 calls will arrive in a given 2 hour period? Give answer to 4 decimals.
    - (b) What is the probability of waiting more than 15 minutes between two calls? (*Hint: 15 minutes = 0.25 hour*)

- (c) What is the probability that there are 22 phone calls in a given hour?
5. Suppose the weight, say,  $Y$ , in pounds of a certain packaged chemical is uniform from 48 to 50 pounds. That is the pdf is of the form

$$f_Y(y) = \frac{1}{2}, \text{ for } 48 < y < 50.$$

- (a) What is the mean weight of the chemical?
- (b) What is the probability that a randomly chosen package of chemical will weigh between 48.5 and 49.4 pounds?
- (c) In the long run, what proportion of packages will weigh more than 49.2 pounds?